The Perception-Distortion Tradeoff

Yochai Blau and Tomer Michaeli
Technion–Israel Institute of Technology, Haifa, Israel
{yochai@campus,tomer.m@ee}.technion.ac.il

Abstract

Image restoration algorithms are typically evaluated by some distortion measure (e.g., PSNR, SSIM, IFC, VIF) or by human opinion scores that quantify perceived perceptual quality. In this paper, we prove mathematically that distortion and perceptual quality are at odds with each other. Specifically, we study the optimal probability for correctly discriminating the outputs of an image restoration algorithm from real images. We show that as the mean distortion decreases, this probability must increase (indicating worse perceptual quality). As opposed to the common belief, this result holds true for any distortion measure, and is not only a problem of the PSNR or SSIM criteria. However, as we show experimentally, for some measures it is less severe (e.g., distance between VGG features). We also show that generative-adversarial-nets (GANs) provide a principled way to approach the perception-distortion bound. This constitutes theoretical support to their observed success in low-level vision tasks. Based on our analysis, we propose a new methodology for evaluating image restoration methods, and use it to perform an extensive comparison between recent super-resolution algorithms.

1. Introduction

The last decades have seen continuous progress in image restoration algorithms (e.g., for denoising, deblurring, super-resolution) both in visual quality and in distortion measures like peak signal-to-noise ratio (PSNR) and structural similarity index (SSIM) [45]. However, in recent years, it seems that the improvement in reconstruction accuracy is not always accompanied by an improvement in visual quality. In fact, and perhaps counter-intuitively, algorithms that are superior in terms of perceptual quality, are often inferior in terms of e.g., PSNR and SSIM [22, 16, 6, 38, 51, 49]. This phenomenon is commonly interpreted as a shortcoming of the existing distortion measures [44], which fuels a constant search for alternative “more perceptual” criteria.

In this paper, we offer a complementary explanation for the apparent tradeoff between perceptual quality and distortion measures. Specifically, we prove that there exists a region in the perception-distortion plane, which cannot be attained regardless of the algorithmic scheme (see Fig. 1). Furthermore, the boundary of this region is monotone. Therefore, in its proximity, it is only possible to improve either perceptual quality or distortion, one at the expense of the other. The perception-distortion tradeoff exists for all distortion measures, and is not only a problem of the mean-square error (MSE) or SSIM criteria. However, for some measures, the tradeoff is weaker than others. For example, we find empirically that the recently proposed distance between deep-net features [16, 22] has a weaker tradeoff with perceptual quality than MSE. This aligns with the observation that this measure is “more perceptual” than MSE.

Let us clarify the difference between distortion and perceptual quality. The goal in image restoration is to estimate an image \( x \) from its degraded version \( y \) (e.g., noisy, blurry, etc.). Distortion refers to the dissimilarity between the reconstructed image \( \hat{x} \) and the original image \( x \). Perceptual
quality, on the other hand, refers only to the visual quality of $\hat{x}$, regardless of its similarity to $x$. Namely, it is the extent to which $\hat{x}$ looks like a valid natural image. An increasingly popular way of measuring perceptual quality is by using real-vs.-fake user studies, which examine the ability of human observers to tell whether $\hat{x}$ is real or the output of an algorithm \cite{15, 53, 39, 8, 6, 14, 54, 11} (similarly to the idea underlying generative adversarial nets \cite{10}). Therefore, perceptual quality can be defined as the best possible probability of success in such discrimination experiments, which as we show, is proportional to the distance between the distribution of $\hat{x}$ and that of natural images.

Based on these definitions of perception and distortion, we follow the logic of rate-distortion theory \cite{4}. That is, we seek to characterize the behavior of the best attainable perceptual quality (minimal deviation from natural image statistics) as a function of the maximal allowable average distortion, for any estimator. This perception-distortion function (wide curve in Fig. 1) separates between the attainable and unattainable regions in the perception-distortion plane and thus describes the fundamental tradeoff between perception and distortion. Our analysis shows that algorithms cannot be simultaneously very accurate and produce images that fool observers to believe they are real, no matter what measure is used to quantify accuracy. This tradeoff implies that optimizing distortion measures can be not only ineffective, but also potentially damaging in terms of visual quality. This has been empirically observed \textit{e.g.} in \cite{22, 16, 38, 51, 6}, but was never established theoretically.

From the standpoint of algorithm design, we show that generative adversarial nets (GANs) provide a principled way to approach the perception-distortion bound. This gives theoretical support to the growing empirical evidence of the advantages of GANs in image restoration \cite{22, 38, 35, 51, 36, 15, 55}.

The perception-distortion tradeoff has major implications on low-level vision. In certain applications, reconstruction accuracy is of key importance (\textit{e.g.} medical imaging). In others, perceptual quality may be preferred. The impossibility of simultaneously achieving both goals calls for a new way for evaluating algorithms: By placing them on the perception-distortion plane. We use this new methodology to conduct an extensive comparison between recent super-resolution (SR) methods, revealing which SR methods lie closest to the perception-distortion bound.

2. Distortion and perceptual quality

Distortion and perceptual quality have been studied in many different contexts, and are sometimes referred to by different names. Let us briefly put past works in our context.

2.1. Distortion (full-reference) measures

Given a distorted image $\hat{x}$ and a ground-truth reference image $x$, full-reference distortion measures quantify the quality of $\hat{x}$ by its discrepancy to $x$. These measures are often called full reference image quality criteria because of the reasoning that if $\hat{x}$ is similar to $x$ and $x$ is of high quality, then $\hat{x}$ is also of high quality. However, as we show in this paper, this logic is not always correct. We thus prefer to call these measures distortion or dissimilarity criteria.

The most common distortion measure is the MSE, which is quite poorly correlated with semantic similarity between images \cite{44}. Many alternative, more perceptual, distortion measures have been proposed over the years, including SSIM \cite{45}, MS-SSIM \cite{47}, IFC \cite{41}, VIF \cite{40}, VSNR \cite{3} and FSIM \cite{52}. Recently, measures based on the $\ell_2$-distance between deep feature maps of a neural-net have been shown to capture more semantic similarities. These measures were used as loss functions in super-resolution and style transfer applications, leading to reconstructions with high visual quality \cite{16, 22, 38}.

2.2. Perceptual quality

The perceptual quality of an image $\hat{x}$ is the degree to which it looks like a natural image, and has nothing to do with its similarity to any reference image. In many image processing domains, perceptual quality has been associated with deviations from natural image statistics.

**Human opinion based quality assessment** Perceptual quality is commonly evaluated empirically by the mean opinion score of human subjects \cite{31, 29}. Recently, it has become increasingly popular to perform such studies through real vs. fake questionnaires \cite{15, 53, 39, 8, 6, 14, 15, 54, 11}. These test the ability of a human observer to distinguish whether an image is real or the output of some algorithm. The probability of success $p_{\text{success}}$, of the optimal decision rule in this hypothesis testing task is known to be

$$p_{\text{success}} = \frac{1}{2} d_{\text{TV}}(p_X, p_{\hat{X}}) + \frac{1}{2},$$

where $d_{\text{TV}}(p_X, p_{\hat{X}})$ is the total-variation (TV) distance between the distribution $p_{\hat{X}}$ of images produced by the algorithm in question, and the distribution $p_X$ of natural images \cite{32}. Note that $p_{\text{success}}$ decreases as the deviation between $p_{\hat{X}}$ and $p_X$ decreases, becoming $\frac{1}{2}$ (no better than a coin toss) when $p_{\hat{X}} = p_X$.

**No-reference quality measures** Perceptual quality can also be measured by an algorithm. In particular, no-reference measures quantify the perceptual quality of an image $\hat{x}$ without depending on a reference image. These measures are commonly based on estimating deviations from natural image statistics. For example, \cite{46, 48, 23} proposed...
a perceptual quality index based on the Kullback-Leibler (KL) divergence between the distribution of the wavelet coefficients of \( \hat{x} \) and that of natural scenes. This idea was further extended by the popular methods DIIVINE [31], BRISQUE [29], BLINDS-II [37] and NIQE [30], which quantify perceptual quality by various measures of deviation from natural image statistics in the spatial, wavelet and DCT domains.

**GAN-based image restoration** Most recently, GAN-based methods have demonstrated unprecedented perceptual quality in super-resolution [22, 38], inpainting [35, 51], compression [36] and image-to-image translation [15, 55]. This was accomplished by utilizing an adversarial loss, which minimizes some distance \( d(p_X, p_{\hat{X}_{\text{GAN}}}) \) between the distribution \( p_{\hat{X}_{\text{GAN}}} \) of images produced by the generator and the distribution \( p_X \) of images in the training dataset. A large variety of GAN schemes have been proposed, which minimize different distances between distributions. These include the Jenson-Shannon divergence [10], the Wasserstein distance [1], and any \( f \)-divergence [34].

### 3. Problem formulation

In statistical terms, a natural image \( x \) can be thought of as a realization from the distribution of natural images \( p_X \). In image restoration, we observe a degraded version \( y \) relating to \( x \) via some conditional distribution \( p_{Y|X} \) (corresponding to noise, blur, down-sampling, etc.). Given \( y \), we produce an estimate \( \hat{x} \) according to some distribution \( p_{\hat{X}|Y} \). This description is quite general in that it does not restrict the estimator \( \hat{x} \) to be a deterministic function of \( y \). This problem setting is illustrated in Fig. 2.

Given a full-reference dissimilarity criterion \( \Delta(x, \hat{x}) \), the average distortion of an estimator \( \hat{X} \) is given by

\[
\mathbb{E}[\Delta(X, \hat{X})],
\]

where the expectation is over the joint distribution \( p_{X, \hat{X}} \).

This definition aligns with the common practice of evaluating average performance over a database of degraded natural images. Note that some distortion measures, e.g. SSIM, are actually similarity measures (higher is better), yet can always be inverted to become dissimilarity measures.

As discussed in Sec. 2.2, the perceptual quality of an estimator \( \hat{X} \) (as quantified e.g. by real vs. fake human opinion studies) is directly related to the distance between the distribution of its reconstructed images \( p_{\hat{X}} \), and the distribution of natural images \( p_X \). We thus define the perceptual quality index (lower is better) of an estimator \( \hat{X} \) as

\[
d(p_X, p_{\hat{X}}),
\]

where \( d(\cdot, \cdot) \) is some divergence between distributions, e.g. the KL divergence, TV distance, Wasserstein distance, etc.

Notice that the best possible perceptual quality is obtained when the outputs of the algorithm follow the distribution of natural images (i.e. \( p_{\hat{X}} = p_X \)). In this situation, by looking at the reconstructed images, it is impossible to tell that they were generated by an algorithm. However, not every estimator with this property is necessarily accurate. Indeed, we could achieve perfect perceptual quality by randomly drawing natural images that have nothing to do with the original “ground-truth” images. In this case the distortion would be quite large.

Our goal is to characterize the tradeoff between (2) and (3). But let us first exemplify why minimizing the average distortion (2), does not necessarily lead to a low perceptual quality index (3). We illustrate this with the square-error distortion \( \Delta(x, \hat{x}) = \| x - \hat{x} \|^2 \) and the 0–1 distortion \( \Delta(x, \hat{x}) = 1 - \delta_{x,\hat{x}} \) (where \( \delta \) is Kronecker’s delta).

### 3.1. The square-error distortion

The minimum mean square-error (MMSE) estimator is given by the posterior-mean \( \hat{x}_{\text{MMSE}}(y) = \mathbb{E}[X|Y = y] \). Consider the case \( Y = X + N \), where \( X \) is a discrete random variable with probability mass function

\[
\hat{x}_{\text{MMSE}}(y) = \sum_{n \in \{-1,0,1\}} n \ p(X = n|y),
\]

where

\[
p(X = n|y) = \frac{p_n \exp\left(-\frac{1}{2}(y - n)^2\right)}{\sum_{m \in \{-1,0,1\}} p_m \exp\left(-\frac{1}{2}(y - m)^2\right)}.
\]
Notice that \( \hat{x}_{\text{MMSE}} \) can take any value in the range \((-1, 1)\), whereas \( x \) can only take the discrete values \([-1, 0, 1]\). Thus, clearly, \( p_{\hat{x}_{\text{MMSE}}} \) is very different from \( p_X \), as illustrated in Fig. 3. This demonstrates that minimizing the MSE distortion does not generally lead to \( p_{\hat{x}} \approx p_X \).

The same intuition holds for images. The MMSE estimate is an average over all possible explanations to the measured data, weighted by their likelihoods. However the average of valid images is not necessarily a valid image, so that the MMSE estimate frequently “falls off” the natural image manifold [22]. This leads to unnatural blurry reconstructions, as illustrated in Fig. 4. In this experiment, \( x \) is a 280 \times 280 image comprising 100 smaller 28 \times 28 digit images. Each digit is chosen uniformly at random from the MNIST dataset [21] and an additional 5.4K blank images. The degraded image \( y \) is a noisy version of \( x \). As can be seen, the MMSE estimator produces blurry reconstructions, which do not follow the statistics of the (binary) images in the dataset.

### 3.2. The 0–1 distortion

The discussion above may give the impression that unnatural estimates are mainly a problem of the square-error distortion, which causes averaging. One way to avoid averaging, is to minimize the binary 0–1 loss, which restricts the estimator to choose \( \hat{x} \) only from the set of values that \( x \) can take. In fact, the minimum mean 0–1 distortion is attained by the maximum-a-posteriori (MAP) rule, which is very popular in image restoration. However, as we exemplify next, the distribution of the MAP estimator also deviates from \( p_X \). This behavior has also been studied in [33].

Consider again the setting of (4). In this case, the MAP estimate is given by

\[
\hat{x}_{\text{MAP}}(y) = \arg \max_{n \in \{-1, 0, 1\}} p(X = n|y),
\]

where \( p(\bar{X} = n|y) \) is as in (6). Now, it can be easily verified that when \( \log(p_{\hat{X}}/p_{\bar{X}}) > 1/2 \), we have \( \hat{x}_{\text{MAP}}(y) = \text{sign}(y) \). Namely, the MAP estimator never predicts the value 0. Therefore, in this case, the distribution of the estimate is

\[
p_{\hat{x}_{\text{MAP}}}({\hat{x}}) = \begin{cases} 0.5 & \hat{x} = +1, \\ 0.5 & \hat{x} = -1, \end{cases}
\]

which is obviously different from \( p_X \) of (4) (see Fig. 3).

This effect can also be seen in the experiment of Fig. 4. Here, the MAP estimator is increasingly dominated by blank images as the noise level rises, and thus clearly deviates from the underlying prior distribution.

### 4. The perception-distortion tradeoff

We saw that low distortion does not generally imply good perceptual-quality. An interesting question, then, is: What is the best perceptual quality that can be attained by an estimator with a prescribed distortion level?

**Definition 1.** The perception-distortion function of a signal restoration task is given by

\[
P(D) = \min_{\hat{X}} \text{d}(p_X, p_{\hat{X}}) \quad \text{s.t.} \quad \mathbb{E}[\Delta(X, \hat{X})] \leq D,
\]

where \( \Delta(\cdot, \cdot) \) is a distortion measure and \( \text{d}(\cdot, \cdot) \) is a divergence between distributions.
In words, \( P(D) \) is the minimal deviation between the distributions \( p_X \) and \( p_\hat{X} \) that can be attained by an estimator with distortion \( D \). To gain intuition into the typical behavior of this function, consider the following example.

**Example 1.** Suppose that \( Y = X + N \), where \( X \sim \mathcal{N}(0, 1) \) and \( N \sim \mathcal{N}(0, \sigma_N) \), and the estimator is linear, \( \hat{X} = aY \). Notice the clear trade-off: The perceptual index \( d_{KL} \) drops as the allowable distortion (MSE) increases. The graphs cut-off at the MMSE (marked by a square).

The convexity of \( P(D) \) implies that the tradeoff is more severe at the low-distortion and at the high-perceptual-quality extremes. This is particularly important when considering the TV divergence which is associated with the ability to distinguish between real vs. fake images (see Sec. 2.2). Since \( P(D) \) is a large degradation in the ability to fool a discriminator. Similarly, any small improvement in the perceptual quality of an algorithm whose perceptual index is already low, must be accompanied by a large increase in distortion. Let us comment that the assumption that \( d(p, q) \) is convex, is not very limiting. For instance, any \( f \)-divergence (e.g. KL, TV, Hellinger, \( \chi^2 \)) as well as the Renyi divergence, satisfy this assumption [5, 43]. In any case, the function \( P(D) \) is monotonically non-increasing even without this assumption.

## 4.1. Connection to rate-distortion theory

The perception-distortion tradeoff is closely related to the well-established rate-distortion theory [4]. This theory characterizes the tradeoff between the bit-rate required to communicate a signal, and the distortion incurred in the signal’s reconstruction at the receiver. More formally, the rate-distortion function of a signal \( X \) is defined by

\[
R(D) = \min_{P_{\hat{X}|X}} I(X; \hat{X}) \quad \text{s.t.} \quad \mathbb{E}[\Delta(X, \hat{X})] \leq D, \quad (10)
\]

where \( I(X; \hat{X}) \) is the mutual information between \( X \) and \( \hat{X} \).

There are, however, several key differences between the two tradeoffs. First, in rate-distortion the optimization is over all conditional distributions \( p_{\hat{X}|X} \), i.e. given the original signal. In the perception-distortion case, the estimator has access only to the degraded signal \( Y \), so that the optimization is over the conditional distributions \( p_{\hat{X}|Y} \), which is more restrictive. In other words, the perception-distortion tradeoff depends on the degradation \( p_{X|Y} \), and not only on the signal’s distribution \( p_X \) (see Example 1). Second, in rate-distortion the rate is quantified by the mutual information \( I(X; \hat{X}) \), which depends on the joint distribution \( p_{X, \hat{X}} \). In our case, perception is quantified by the similarity between \( p_X \) and \( p_{\hat{X}} \), which does not depend on their joint distribution. Lastly, mutual information is inherently convex, while the convexity of the perception-distortion curve is guaranteed only when \( d(\cdot, \cdot) \) is convex.

## 5. Traversing the tradeoff with a GAN

There exists a systematic way to design estimators that approach the perception-distortion curve: Using GANs. Specifically, motivated by [22, 35, 51, 38, 36, 15], restoration problems can be approached by modifying the loss of...
the generator of a GAN to be
\[ \ell_{\text{gen}} = \ell_{\text{distortion}} + \lambda \ell_{\text{adv}}, \quad (11) \]
where \( \ell_{\text{distortion}} \) is the distortion between the original and reconstructed images, and \( \ell_{\text{adv}} \) is the standard GAN adversarial loss. It is well known that \( \ell_{\text{adv}} \) is proportional to some divergence \( d(p_X, p_{\hat{X}}) \) between the generator and data distributions \([10, 1, 34]\) (the type of divergence depends on the loss). Thus, (11) in fact approximates the objective
\[ \ell_{\text{gen}} \approx E[\Delta(x, \hat{x})] + \lambda d(p_X, p_{\hat{X}}). \quad (12) \]
Viewing \( \lambda \) as a Lagrange multiplier, it is clear that minimizing \( \ell_{\text{gen}} \) is equivalent to minimizing (9) for some \( D \). Varying \( \lambda \) correspond to varying \( D \), thus producing estimators along the perception-distortion function.

Let us use this approach to explore the perception-distortion tradeoff for the digit denoising example of Fig. 4 with \( \sigma = 3 \). We train a Wasserstein GAN (WGAN) based denoiser \([1, 12]\) with an MSE distortion loss \( \ell_{\text{distortion}} \). Here, \( \ell_{\text{adv}} \) is proportional to the Wasserstein distance \( d_{\text{W}}(p_X, p_{\hat{X}}) \) between the generator and data distributions. The WGAN has the valuable property that its discriminator (critic) loss is an accurate estimate (up to a constant factor) of \( d_{\text{W}}(p_X, p_{\hat{X}}) \) \([1]\). This allows us to easily compute the perceptual quality index of the trained denoiser. We obtain a set of estimators with several values of \( \lambda \in [0, 0.3] \). For each denoiser, we evaluate the perceptual quality by the final discriminator loss.

Figure 6. Image denoising utilizing a GAN. A Wasserstein GAN was trained to denoise the images of the experiment in Fig. 4. The generator loss \( \ell_{\text{gen}} = \ell_{\text{MSE}} + \lambda \ell_{\text{adv}} \) consists of a perceptual quality (adversarial) loss and a distortion (MSE) loss, where \( \lambda \) controls the trade-off between the two. For each \( \lambda \in [0, 0.3] \), the graph depicts the distortion (MSE) and perceptual quality (Wasserstein distance between \( p_X \) and \( p_{\hat{X}} \)). The curve connecting the estimators is a good approximation to the theoretical perception-distortion tradeoff (illustrated by a dashed line).

Figure 7. Dominance and admissibility. Algorithm A is dominated by Algorithm B, and is thus inadmissible. Algorithms B, C and D are all admissible, as they are not dominated by any algorithm.

6. Practical method for evaluating algorithms

Certain applications may require low-distortion (e.g. in medical imaging), while others may prefer superior perceptual quality. How should image restoration algorithms be evaluated, then?

**Definition 2.** We say that Algorithm A dominates Algorithm B if it has better perceptual quality and less distortion.

Note that if Algorithm A is better than B in only one of the two criteria, then neither A dominates B nor B dominates A. Therefore, among a group of algorithms, there may be a large subset which can be considered equally good.
Figure 8. Perception-distortion evaluation of SR algorithms. We plot 16 algorithms on the perception-distortion plane. Perception is measured by the recent NR metric by Ma et al. [26] which is specifically designed for SR quality assessment. Distortion is measured by the common full-reference metrics RMSE, SSIM, MS-SSIM, IFC, VIF and VGG2. In all plots, the lower left corner is blank, revealing an unattainable region in the perception-distortion plane. In proximity of the unattainable region, an improvement in perceptual quality comes at the expense of higher distortion.

**Definition 3.** We say that an algorithm is **admissible** among a group of algorithms, if it is not dominated by any other algorithm in the group.

As shown in Figure 7, these definitions have very simple interpretations when plotting algorithms on the perception-distortion plane. In particular, the admissible algorithms in the group, are those which lie closest to the perception-distortion bound.

As discussed in Sec. 2, distortion is measured by full-reference (FR) metrics, *e.g.* [45, 47, 41, 40, 3, 52, 16]. The choice of the FR metric, depends on the type of similarities we want to measure (per-pixel, semantic, etc.). Perceptual quality, on the other hand, is ideally quantified by collecting human opinion scores, which is time consuming and costly [31, 37]. Instead, the divergence $d(p_X, \hat{p}_X)$ can be computed, for instance by training a discriminator net (see Sec. 5). However, this requires many training images and is thus also time consuming. A practical alternative is to utilize no-reference (NR) metrics, *e.g.* [29, 30, 37, 31, 50, 17, 26], which quantify the perceptual quality of an image without a corresponding original image. In scenarios where NR metrics are highly correlated with human mean-opinion-scores (*e.g.* 4× super-resolution [26]), they can be used as a fast and simple method for approximating the perceptual quality of an algorithm.

We use this approach to evaluate 16 SR algorithms in a 4× magnification task, by plotting them on the perception-distortion plane (Fig. 8). We measure perceptual quality using the recent NR metric by Ma et al. [26] which is specifically designed for SR quality assessment (see Supplementary for experiments with the NR metrics BRISQUE [29], NIQE [30] and BLIINDS-II [37]). We measure distortion by the five common FR metrics RMSE, SSIM [45], MS-SSIM [47], IFC [41] and VIF [40], and additionally by the recent VGG2 metric (the distance in the feature space of a VGG net) [22, 16]. To conform to previous evaluations, we compute all metrics on the y-channel after discarding a 4-pixel border (except for VGG2, which is computed on RGB images). Comparisons on color images can be found in the Supplementary. The algorithms are evaluated on the BSD100 dataset [27]. The evaluated algorithms include: A+ [42], SRCNN [9], SelfEx [13], VDSR [18], Johnson et al. [16], LapSRN [19], Bae et al. [2] (“primary” variant), EDSR [24], SRResNet variants which optimize MSE.
and VGG$_{2,2}$ [22], SRGAN variants which optimize MSE, VGG$_{2,2}$, and VGG$_{5,4}$, in addition to an adversarial loss [22], ENet [38] (“PAT” variant), Deng [7] ($\gamma = 0.55$), and Mechrez et al. [28].

Interestingly, the same pattern is observed in all plots: (i) The lower left corner is blank, revealing an unattainable region in the perception-distortion plane. (ii) In proximity of this blank region, NR and FR metrics are anti-correlated, indicating a tradeoff between perception and distortion. Notice that the tradeoff exists even for the IFC and VIF measures, which are considered to capture visual quality better than MSE and SSIM. The tradeoff is evident also for the VGG$_{2,2}$ measure, but is somewhat weaker than for MSE. This may indicate that VGG$_{2,2}$ is a more “perceptual” metric. It should be noted, however, that when using other NR metrics to measure perceptual quality, the tradeoff for VGG$_{2,2}$ does not appear to be weaker (see Supplementary). This is due to the sensitivity of some of the NR metrics to the periodic artifacts that arise when minimizing the VGG$_{2,2}$ distortion$^3$ (see Fig. 9).

Figure 9 depicts the outputs of several algorithms lying closest to the perception-distortion bound in the IFC graph. While the images are ordered from low to high distortion (according to IFC), their perceptual quality clearly improves from left to right.

Both FR and NR measures are commonly validated by calculating their correlation with human opinion scores, based on the assumption that both should be correlated with perceptual quality. However, as Fig. 10 shows, while FR measures can be well-correlated with perceptual quality when distant from the unattainable region, this is clearly not the case when approaching the perception-distortion bound. In particular, all tested FR methods are inconsistent with human opinion scores which found the SRGAN to be super in terms of perceptual quality [22], while NR methods successfully determine this. We conclude that image restoration algorithms should always be evaluated by a pair of NR and FR metrics, constituting a reliable, reproducible and simple method for comparison, which accounts for both perceptual quality and distortion.

$^3$Minimizing VGG$_{2,2}$ (as done by SRResNet-VGG$_{2,2}$), leads to sharper images (compared to minimizing MSE) but with periodic artifacts [16]. Different NR metrics have different sensitivities to these artifacts.

Figure 9. Visual comparison of algorithms closest to the perception-distortion bound. The algorithms are ordered from low to high distortion (evaluated by IFC). Notice the co-occurring increase in perceptual quality.

Figure 10. Correlation between distortion and perceptual quality. In proximity of the perception-distortion bound, distortion and perceptual quality are anti-correlated. However, correlation is possible at distance from the bound.

Up until 2016, SR algorithms occupied only the upper-left section of the perception-distortion plane. Nowadays, emerging techniques are exploring new regions in this plane. The SRGAN, ENet, Deng, Johnson et al. and Mechrez et al. methods are the first (to our knowledge) to populate the high perceptual quality region. In the near future we will most likely witness continued efforts to approach the perception-distortion bound, not only in the low-distortion region, but throughout the entire plane.

7. Conclusion

We proved and demonstrated the counter-intuitive phenomenon that distortion and perceptual quality are at odds with each other. Namely, the lower the distortion of an algorithm, the more its distribution must deviate from the statistics of natural scenes. We showed empirically that this tradeoff exists for many popular distortion measures, including those considered to be well-correlated with human perception. Therefore, any distortion measure alone, is unsuitable for assessing image restoration methods. Our novel methodology utilizes a pair of NR and FR metrics to place each algorithm on the perception-distortion plane, facilitating a more informative comparison of image restoration methods.

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